

1: For each problem below, a shape and a dot (\bullet) are given to you. This dot represents one vertex of a tessellation made by the shape. Fill in this tessellation around the vertex.

1. Squares:



2. Regular triangles (recall that regular means all of the internal angles are the same):



3. Regular hexagons:



4. Identical rectangles that are not squares:



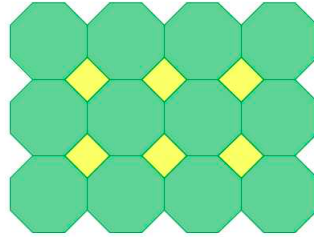
2: We will denote by N the **Number of shapes that meet at one vertex**. Using your tessellations from problem 1, Fill in the following table. The last one has been done for you.

Shape	Internal Angle	N	$N \times \text{InternalAngle}$
Square			
Regular Triangle			
Regular Hexagon			
Rectangle	90	4	360

3: Use the dot below to draw a tessellation consisting of pentagons (5 sides). Prove that there does not exist a tessellation that uses only *regular* pentagons.



4: In this problem we consider *semi-tessellations*. These are different than tessellations in that we can use two shapes instead of one. The rule is still that every vertex must look the same.

Example 1. *Octagons and Squares*

Repeat what you did in problem 1 for the semi-tessellations below. **All shapes below are assumed to be regular!**

1. triangles and hexagons (there are two different ways of doing this, hence the two dots).

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2. Triangles and squares (there are also two different ways of doing this.)

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3. Triangles, squares, and hexagons.

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4. Triangles and dodecagons (12 sides)

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5. Squares, hexagons, and dodecagons

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5: